

Math 112: #2 A/B

1. Suppose Dr. Evil's spaceship is in lunarsynchronous orbit around the Moon. It remains above the same point on the moon's equator about $88,000\text{ km}$ above the surface. Assuming the radius of the moon is $1,737\text{ km}$. Find the following. State the exact answer, then give a decimal answer rounded to ~~two~~⁴ decimal places.

- a. The angular speed of the spaceship in radians per hour.

a moonday is ~ 27 earth days

$$\text{Angular Speed} = \omega = \frac{\theta}{t} = \frac{2\pi}{27 \cdot 24} = \frac{\pi}{27 \cdot 12} = \frac{\pi}{324} \text{ radians/hour}$$

$$= 0.0097 \text{ radians/hour}$$



$$r_1 = 1737 \text{ km}$$

$$r_2 = 88,000 \text{ km}$$

- b. The linear speed of the spaceship in kilometers per hour.

$$\text{linear speed} = v = \frac{s}{t} \quad \text{arc length} \quad s = r\theta = (88,000 + 1,737) \text{ km} \cdot 2\pi$$

$$v = \frac{179,474\pi \text{ km}}{27 \cdot 24 \text{ hr}} = 276.97\pi \text{ km/hr}$$

$$= 870.11 \text{ km/hr}$$

2. Find the distance that the earth travels in one day in its path around the sun. Assume that a year has 365 days and that the path of the earth around the sun is a circle of radius of 93 million miles. State the exact answer, then give a decimal answer rounded to two decimal places.



$$S = r\theta$$

$$S = 93,000,000 \cdot 2\pi = \text{distance/year}$$

$$\frac{S}{365} = \text{distance/day} = \frac{93,000,000 \cdot 2\pi \text{ miles/year}}{365 \text{ days/year}}$$

$$= 509589.0411 \pi \text{ miles/day}$$

$$= 1,600,921.19 \text{ miles/day}$$