

D
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$(-3, 6)$ to $(2, -4)$ $\Delta x = 5$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-4 - 6}{2 - (-3)} = \frac{-10}{5} = -2$$

$$x(t) = x_1 + bt$$

$$y(t) = y_1 + at$$

$$m = \frac{a}{b} \quad 0 \leq t \leq$$

#1

$$\begin{aligned} x &= -3 + 1t \\ y &= 6 - 2t \quad 0 \leq t \leq 5 \end{aligned}$$

#2

$$\begin{aligned} x &= -3 + 5t \\ y &= 6 - 10t \quad 0 \leq t \leq 1 \end{aligned}$$

B
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Part I

$$x(t) = 3 \sin t \quad y(t) = 2 \cos t$$

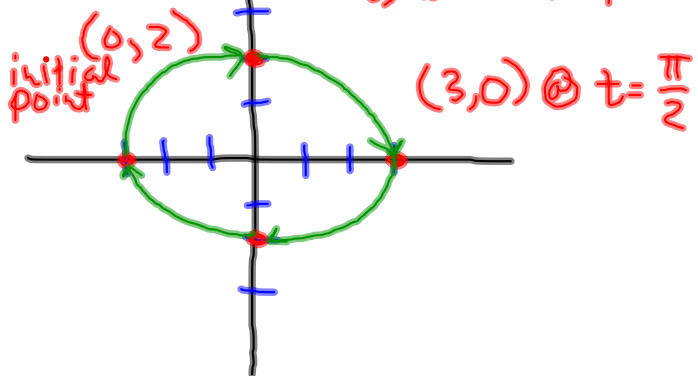
$$0 \leq t \leq 2\pi$$

1) initial point

2) point at $\frac{\pi}{2} = t$

3) Direction

t	x	y
0	0	2
$\frac{\pi}{2}$	3	0
π	0	-2
$\frac{3\pi}{2}$	-3	0
2π	0	2



Part II

$$\frac{x}{3} = \frac{3\sin t}{3} \quad \frac{y}{2} = \frac{2\cos t}{2}$$

$$\frac{x}{3} = \sin t \quad \frac{y}{2} = \cos t$$

$$\sin^2 t + \cos^2 t = 1$$

$$\left(\frac{x}{3}\right)^2 + \left(\frac{y}{2}\right)^2 = 1$$

$$36 \cdot \left(\frac{x^2}{9} + \frac{y^2}{4}\right) = 1 \cdot 36$$

$$4x^2 + 9y^2 = 36$$

Ellipses

~~31~~

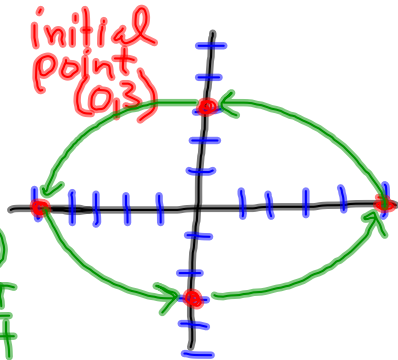
$$x(t) = -5\sin 2t \quad y(t) = 3\cos 2t$$

$$0 \leq t \leq \pi$$

$$t = \frac{\pi}{4}$$

t	x	y
0	0	3
$\pi/4$	-5	0
$\pi/2$	0	-3
$3\pi/4$	5	0
π	0	3

(-5, 0)
@ $t = \frac{\pi}{4}$



$$x = -5 \sin 2t \quad y = 3 \cos 2t$$

$$x = -5 \sin \theta \quad y = 3 \cos \theta \quad \text{let } \theta = 2t$$

$$\frac{x}{-5} = \sin \theta \quad \frac{y}{3} = \cos \theta$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\left(\frac{x}{-5}\right)^2 + \left(\frac{y}{3}\right)^2 = 1$$

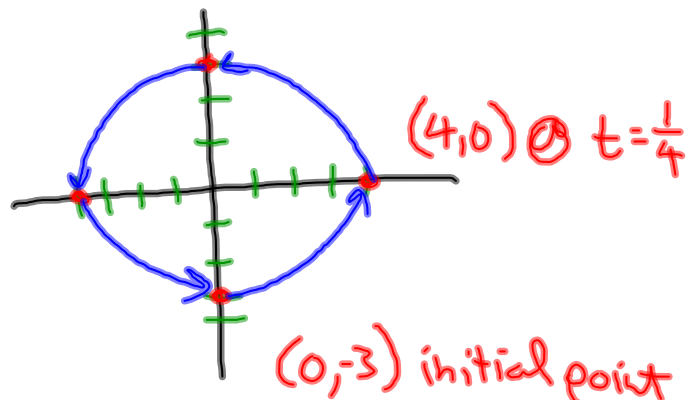
D
31

$$x(t) = 4 \sin 2\pi t \quad y(t) = -3 \cos 2\pi t$$

$$0 \leq t \leq 1$$

$$t = \frac{1}{4}$$

t	x	y
0	0	-3
1/4	4	0
1/2	0	3
3/4	-4	0
1	0	-3



$$\text{let } \theta = 2\pi t$$

$$x = 4 \sin \theta \quad y = -3 \cos \theta$$

$$\frac{x}{4} = \sin \theta \quad \frac{y}{-3} = \cos \theta$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\left(\frac{x}{4}\right)^2 + \left(\frac{y}{-3}\right)^2 = 1$$

3/2

$$(-1, -4) \text{ to } (3, 12)$$

$$\Delta x = 4$$

$$m = \frac{12 - (-4)}{3 - (-1)} = \frac{16}{4} = 4$$

$$x = -1 + 2t$$

$$y = -4 + 8t \quad 0 \leq t \leq 2$$