

Name Mine

Date _____

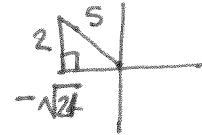
Math 112: Quiz 6.3, 6.4:

show any relevant work.

1. If $\sin \theta = \frac{2}{5}$ and $\cos \theta < 0$, find the value of the other 5 elementary trigonometric functions at θ . Draw a sketch with appropriate reference triangle.

$$\sin \theta = \frac{2}{5}$$

$$\csc \theta = \frac{5}{2}$$



$$\cos \theta = -\frac{\sqrt{21}}{5}$$

$$\sec \theta = -\frac{5\sqrt{21}}{21}$$

$$2^2 + b^2 = 5^2$$

$$4 + b^2 = 25$$

$$b^2 = 21$$

$$b = \sqrt{21}$$

$$= -\sqrt{21}$$

since
 $\cos \theta < 0$

$$\tan \theta = -\frac{2\sqrt{21}}{21}$$

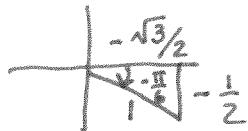
$$\cot \theta = -\frac{\sqrt{21}}{2}$$

$$\cos \theta = -\frac{2}{5}$$

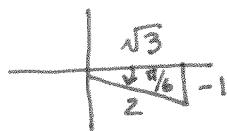
$$\sin \theta = \frac{2}{5}$$

2. Find the exact value of each of the following. Include a circle sketch and reference triangle.

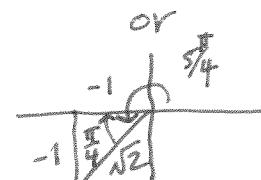
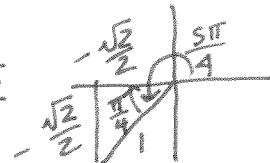
a) $\tan(-\frac{\pi}{6})$
= $-\frac{\sqrt{3}}{3}$



or



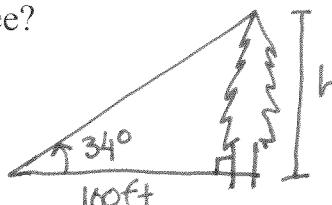
b. $\csc(\frac{5\pi}{4})$
= $-\frac{\sqrt{2}}{1} = -\sqrt{2}$



3. A ponderosa pine casts a shadow of 160 ft on level ground when the angle of elevation to the sun is 34° . How tall is the tree?

$$\sin 34^\circ = \frac{h}{160}$$

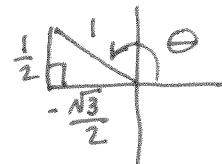
$$160 \sin 34^\circ = h = 89.5 \text{ ft}$$



4. Find the exact value of each of the following. Include a reference triangle.

a) $\cos^{-1}(-\frac{\sqrt{3}}{2}) = \theta$

$$\theta = \frac{5\pi}{6}$$

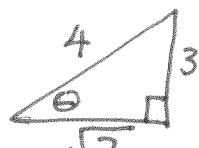


b) $\cos(\sin^{-1}(\frac{3}{4}))$

$$\sin^{-1} \frac{3}{4} = \theta$$

$$\text{so } \sin \theta = \frac{3}{4}$$

$$\cos \theta = \frac{\sqrt{7}}{4}$$



$$3^2 + b^2 = 4^2$$

$$9 + b^2 = 16$$

$$b^2 = 7$$