

Practice 8.4: **Sum & Difference Formulas**

Use the Sum and Difference Formulas to find the exact values of the following trig functions. Show your work.

1. $\cos 75^\circ$ *use $30^\circ + 45^\circ = 75^\circ$*

2. $\sin 15^\circ$ *use $45^\circ - 30^\circ = 15^\circ$*

3. $\tan 105^\circ$ *use $60^\circ + 45^\circ = 105^\circ$*

4. $\cos 195^\circ$ *use $225^\circ - 30^\circ = 195^\circ$*

5. $\sin \frac{7\pi}{12}$ *use $\frac{\pi}{3} + \frac{\pi}{4} = \frac{7\pi}{12}$*

6. $\tan 255^\circ$ *use $300^\circ - 45^\circ = 255^\circ$*

7. Use the Sum and Difference Formulas to write the trig function of an angle.

a. $\cos 25^\circ \cos 15^\circ - \sin 25^\circ \sin 15^\circ =$

b. $\sin 140^\circ \cos 50^\circ - \cos 140^\circ \sin 50^\circ =$

c. $\frac{\tan 325^\circ - \tan 86^\circ}{1 + \tan 325^\circ \tan 86^\circ} =$

d. $\cos \frac{\pi}{7} \cos \frac{\pi}{5} - \sin \frac{\pi}{7} \sin \frac{\pi}{5} =$

8. Find the exact value of the trig functions given that.

$$\sin u = \frac{5}{13} \quad 0 < u < \frac{\pi}{2} \quad \text{and} \quad \cos v = -\frac{3}{5} \quad \frac{\pi}{2} < v < \pi$$

a. $\sin(u + v)$

b. $\cos(u + v)$

c. $\sin(u - v)$

d. $\cos(u - v)$

9. Find the exact value of the trig functions given that.

$$\sin u = \frac{7}{25} \quad \frac{\pi}{2} < u < \pi \quad \text{and} \quad \cos v = \frac{4}{5} \quad \frac{3\pi}{2} < v < 2\pi$$

a. $\sin(u + v)$

b. $\cos(u + v)$

c. $\sin(u - v)$

d. $\cos(u - v)$

Verify the identities.

10. $\sin\left(\frac{\pi}{2} + x\right) = \cos x$

11. $\sin(3\pi - x) = \sin x$

12. $\cos(\pi - \theta) + \sin\left(\frac{\pi}{2} + \theta\right) = 0$

13. $\cos(x + y)\cos(x - y) = \cos^2 x - \sin^2 y$

14. $\sin(x + y) + \sin(x - y) = 2 \sin x \cos y$