

Section 5.3: Properties of logs

Change of Base Formula

common log \rightarrow base 10

natural log (ln) \rightarrow base e

$$\log_a(x) = \frac{\log_b(x)}{\log_b(a)} \rightarrow b = \begin{matrix} \text{new} \\ \text{base} \end{matrix}$$

$$\log_2(32) = \frac{\log(32)}{\log(2)} = \frac{1.505}{0.301} = 5$$

$$\log_2(32) = \frac{\ln(32)}{\ln(2)} = \frac{3.4657}{0.6931} = 5$$

Properties of Logs

Exponent Rules \rightarrow
$$\begin{cases} x^m \cdot x^n = x^{m+n} \\ x^m / x^n = x^{m-n} \\ (x^m)^n = x^{mn} \end{cases}$$

- $\log_a(uv) = \log_a(u) + \log_a(v)$
- $\log_a\left(\frac{u}{v}\right) = \log_a(u) - \log_a(v)$
- $\log_a(x)^u = u \log_a(x)$

ex: $\log\left(\frac{xy}{zz}\right) = \log(x) + \log(y) - \log(z) - \log(z)$

$$\log(x) + \log(y) - [\log(z) + \log(z)]$$

$$\log(x) + \log(y) - \log(z) - \log(z)$$

- $\ln(uv) = \ln(u) + \ln(v)$
- $\ln\left(\frac{u}{v}\right) = \ln(u) - \ln(v)$
- $\ln(x^u) = u\ln(x)$

ex: $\ln(x) + \ln(y) - \frac{1}{2}\ln(z)$
 $\ln(xy) - \ln(z^{\frac{1}{2}})$
 $\ln\left(\frac{xy}{\sqrt{z}}\right)$