

4. (6 points) For what values of x is $\cos^{-1}(\cos x) = x$?

+1 ✓

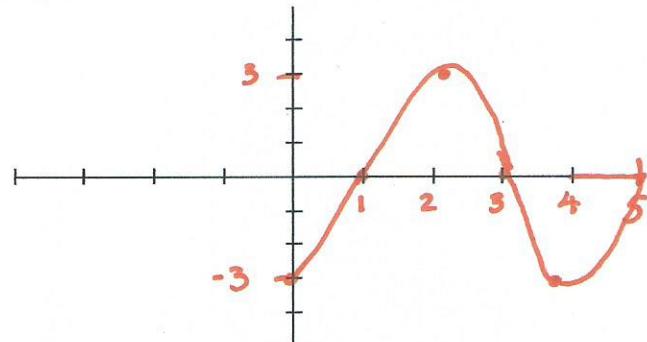
$[0, \pi]$
(6 pts)

5. (16 points) For each of the following functions, sketch one period of the graph carefully. Label the grid sufficiently to indicate the period, amplitude and asymptotes.

a. $f(x) = 3\sin\frac{\pi}{2}(x-1)$

amp ↑
k ↑ phase shift right 1

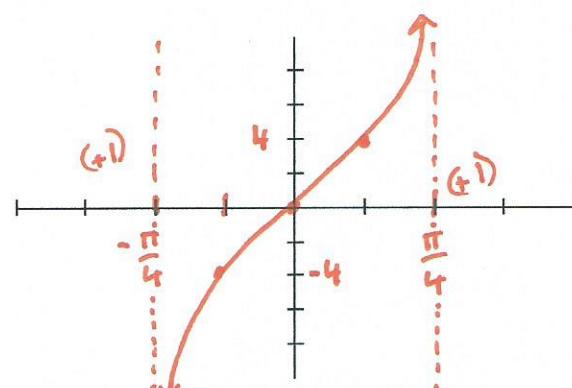
period = $\frac{2\pi}{k} = \frac{2\pi}{\pi/2} = 4$



b. $f(x) = 4\tan(2x)$

amp ↑
k ↑

period = $\frac{\pi}{k} = \frac{\pi}{2}$



6. (16 points) Find the exact values of each of the following. Include a reference angle sketch.

+5 a. $\cos^{-1}\left(\frac{1}{2}\right)$

✓ $\frac{1}{2}, \frac{\sqrt{3}}{2}$

✓ $\frac{\pi}{3}$

(1 pt)

~~sin~~ $\cos \frac{\pi}{3} = \frac{1}{2}$

$\cos^{-1}\left(\frac{1}{2}\right) = \frac{\pi}{3}$

(3 pts)

+5 b. $\sin^{-1}(\cos(\frac{4\pi}{3}))$

✓ $\frac{4\pi}{3}$

✓ $(+2 \text{ pts})$

$\cos \frac{4\pi}{3} = -\frac{1}{2}$

$\sin^{-1}(-\frac{1}{2}) = -\frac{\pi}{6}$ (+3 pts)

+6 c. $\tan^{-1}(\tan(\frac{5\pi}{6}))$

✓ $\frac{5\pi}{6}$

(+3 pts)

$\tan \frac{5\pi}{6} = -\frac{\sqrt{3}}{3}$

$\tan^{-1}(-\frac{\sqrt{3}}{3}) = -\frac{\pi}{6}$ (+3 pts)

$\frac{36}{36}$