

Standard 4 Review:

Name: _____

1. Find the Domain of the following functions.

a. $f(x) = 3x^2 + 7x - 11$

Any real number

c. $h(x) = \sqrt{x-7}$

$x \geq 7$

b. $g(x) = \frac{2x}{x^2 - 4}$

$x \neq \pm 2$

d. $j(x) = \frac{\sqrt{x+3}}{x^2 - 11x + 28}$

$x \geq -3$ and $x \neq 4, 7$

2. Simplify.

a. $\frac{x-5}{x^2 - 25} = \frac{1}{x+5}$

b. $\frac{x^2 - 5x - 14}{x-2} = \frac{(x-7)(x+2)}{(x-2)}$ simplified

c. $\frac{x^2 + 6x - 27}{x^2 - 1} = \frac{x+9}{x-10}$

d. $\frac{x^2}{x^2 + x} = \frac{x}{x+1}$

3. Multiply or Divide and Simplify.

a. $\frac{x^2 + 4x}{x^2 - 16} \cdot \frac{x-4}{x} = 1$

b. $\frac{x^2 + 6x + 8}{x^2 + x - 12} \cdot \frac{x^2 - 9}{x+2} = x+3$

c. $\frac{x^2 + 5x + 6}{x^2 - 8x - 33} \div \frac{x^2 + 8x + 12}{x+6}$

$$= \frac{1}{x-11}$$

d. $\frac{x^2 - 5x - 14}{x^2 - 36} \div \frac{x^2 - 7x - 18}{x^2 - 15x + 54}$

$$= \frac{x-7}{x+6}$$

4. Add or Subtract and Simplify.

a. $\frac{8}{x+2} + \frac{x}{x-3} = \frac{(x+2)(x-2)}{(x+2)(x-3)}$

b. $\frac{x-4}{x-8} - \frac{40}{x^2 - 6x - 16} = \frac{x+6}{x+2}$

c. $\frac{6}{x^2 + 2x - 8} + \frac{1}{x^2 - 5x + 6}$

$$= \frac{7}{(x+4)(x-3)}$$

d. $\frac{x+1}{x^2 + 4x - 5} - \frac{2}{x^2 + 8x + 15}$

$$= \frac{x^2 + 2x + 5}{(x+5)(x-1)(x+3)}$$

5. Simplify.

$$\text{a. } \frac{3 + \frac{9}{x-3}}{4 + \frac{12}{x-3}} = \frac{3}{4}$$

$$\text{b. } \frac{\frac{1}{x+2} + \frac{2}{x}}{\frac{4}{x} + \frac{2}{x(x+2)}} = \frac{3x+4}{2(x+5)}$$

6. Solve.

$$\text{a. } \frac{3x+2}{2} = \frac{1}{4} \\ x = -\frac{1}{2}$$

$$\text{b. } x + \frac{x}{6} + \frac{x}{3} = 3 \\ x = 2$$

$$\text{c. } 3x - \frac{x-2}{4} + 6 = \frac{x+7}{5} \\ x = -2$$

$$\text{d. } \frac{10}{x-2} = 5 \\ x = 4$$

$$\text{e. } \frac{2x}{x-3} + \frac{x+3}{4} = 0$$

$$x = -9, 1$$

$$\text{f. } 1 + \frac{2}{x+2} + \frac{4}{x-2} = 0$$

$$x = 0, 6$$

$$\text{g. } \frac{5}{x+3} - \frac{3}{x} = \frac{1}{3x}$$

$$x = 6$$

$$\text{h. } \frac{x}{x+5} + \frac{1}{x-3} = \frac{13}{x^2 + 2x - 15}$$

$$x = 4, -2$$

$$\text{i. } \frac{x+2}{x} = \frac{2}{x-1}$$

$$x = 2, -1$$

$$\text{j. } \frac{6}{x+4} = \frac{2}{3(x-2)}$$

$$x = 2.75$$

7. Solve.

a. $\frac{x+1}{x-4} \geq 0$

$(-\infty, -1] \text{ and } (4, \infty)$

b. $\frac{x^2 - 4}{x} < 0$

$(-\infty, -2) \text{ and } (0, 2)$

c. $\frac{x^2 + x - 6}{x+1} > 0$

$(-3, -1) \text{ and } (2, \infty)$

d. $\frac{x-4}{x} \leq 2$

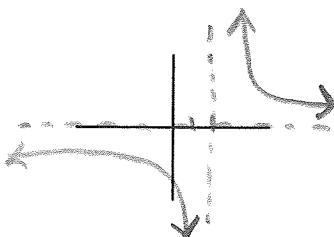
$(-\infty, -4] \text{ and } (0, \infty)$

8. Find the equations for all the Vertical, Horizontal and Slant Asymptotes of the following Rational Functions. Use them to sketch a graph of the function.

a. $f(x) = \frac{1}{x-2}$

V: $x=2$

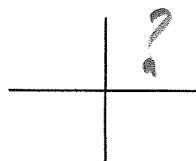
H/S: $y=0$



b. $g(x) = \frac{x^4}{x^2 + 4}$

V: none

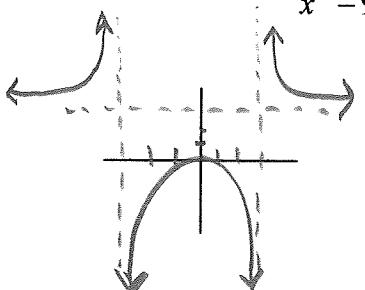
H/S: none



c. $h(x) = \frac{3x^2}{x^2 - 9}$

V: $x=3, x=-3$

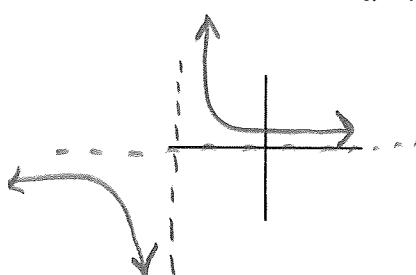
H/S: $y=3$



d. $j(x) = \frac{2x-4}{x^2 + 4x - 12}$

V: $x=-6$

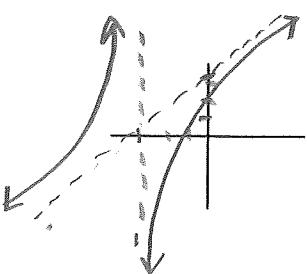
H/S: $y=0$



e. $f(x) = \frac{x^2 + 6x + 8}{x+3}$

V: $x=-3$

H/S: $y=x+3$



f. $k(x) = \frac{2x+8}{4x-16}$

V: $x=4$

H/S: $y = \frac{1}{2}$

