

Practice 7.3: Trig Functions & The Unit Circle

1. Find the point on the unit circle that corresponds to the angle.

a. $\frac{\pi}{4} \left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$ b. $\frac{3\pi}{2} (0, -1)$ c. $-\frac{4\pi}{3} \left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ d. $\frac{11\pi}{6} \left(\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

e. $30^\circ \left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$ f. $135^\circ \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$ g. $300^\circ \left(\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ h. $210^\circ \left(-\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

2. Find the sine, cosine and tangent of the angle.

a. $\frac{5\pi}{4}$

$\sin\left(\frac{5\pi}{4}\right) = -\frac{\sqrt{2}}{2}$
 $\cos\left(\frac{5\pi}{4}\right) = -\frac{\sqrt{2}}{2}$
 $\tan(\) = 1$

b. 150°

$\sin 150^\circ = +\frac{1}{2}$
 $\cos 150^\circ = -\frac{\sqrt{3}}{2}$
 $\tan 150^\circ = -\frac{\sqrt{3}}{3}$

c. $\frac{3\pi}{2}$

$\sin(\) = -1$
 $\cos(\) = 0$
 $\tan(\) = \text{undefined}$

d. 330°

$\sin(\) = -\frac{1}{2}$
 $\cos(\) = \frac{\sqrt{3}}{2}$
 $\tan(\) = -\frac{\sqrt{3}}{3}$

3. Find the value of all 6 trig functions for each angle.

a. $\frac{7\pi}{6}$ $\sin(\) = -\frac{1}{2}$ $\csc(\) = -2$ $\cos(\) = -\frac{\sqrt{3}}{2}$ $\sec(\) = -\frac{2\sqrt{3}}{3}$ $\tan(\) = \frac{\sqrt{3}}{3}$ $\cot(\) = \sqrt{3}$

b. -240° $\sin(\) = \frac{\sqrt{3}}{2}$ $\csc(\) = \frac{2\sqrt{3}}{3}$ $\cos(\) = -\frac{1}{2}$ $\sec(\) = -2$ $\tan(\) = -\sqrt{3}$ $\cot(\) = -\frac{\sqrt{3}}{3}$

4. Use the period to help evaluate the following trig functions.

a. $\sin 3\pi = \sin \pi = 0$ b. $\cos(405^\circ) = \cos(45^\circ) = \frac{\sqrt{2}}{2}$ c. $\tan \frac{25\pi}{6} = \tan \frac{\pi}{6} = \frac{\sqrt{3}}{3}$ d. $\csc(-600^\circ) = \csc(-240^\circ) = \csc 120^\circ = \frac{1}{\sin 120^\circ} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2\sqrt{3}}{3}$

Use the value of the given function to evaluate the remaining ones.

5. $\sin \theta = \frac{1}{3}$

a. $\sin -\theta = -\frac{1}{3}$

b. $\csc \theta = \frac{3}{1} = 3$

6. $\cos(-\theta) = \frac{2}{5}$

a. $\cos \theta = \frac{2}{5}$

b. $\sec \theta = \frac{5}{2}$

7. $\tan(\theta) = \frac{3}{4}$

a. $\tan -\theta = -\frac{3}{4}$

b. $\cot \theta = \frac{4}{3}$

Use the value of the given function to evaluate the remaining ones.

8. $\sin \theta = \frac{2}{3}$



a. $\sin(\pi - \theta) = \frac{2}{3}$

b. $\sin(\pi + \theta) = -\frac{2}{3}$

9. $\cos \theta = \frac{3}{7}$



a. $\cos(\pi - \theta) = -\frac{3}{7}$

b. $\cos(\pi + \theta) = -\frac{3}{7}$

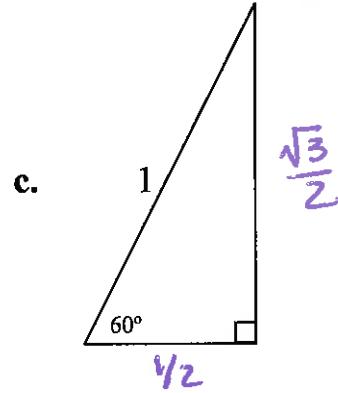
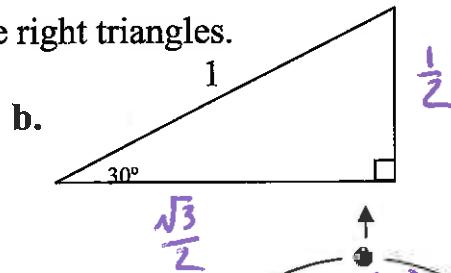
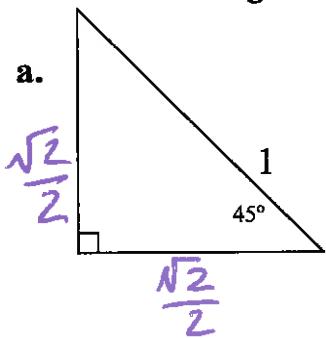


10. Use a calculator to evaluate the trig functions.

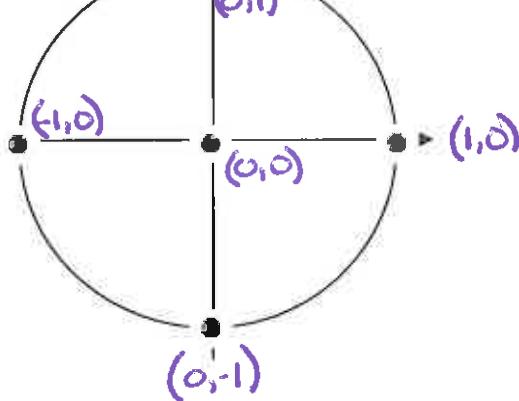
a. $\sin \frac{\pi}{4} = 0.707$ b. $\tan(180^\circ) = 0$ c. $\cos(34.2^\circ) = .83$ d. $\cot(1) = 0.642$

e. $\tan(110.5^\circ) = -2.67$ f. $\sec(54.9^\circ) = 1.74$ g. $\csc(0.8) = 1.39$ h. $\sin(-\frac{5\pi}{3}) = 0.866$

11. Find the missing sides of the right triangles.



12. Find the points on the Unit Circle.



13. Find both the triangle and Unit Circle definition for all 6 trig functions.

a. $\sin \theta = \frac{O}{H} = y$

b. $\csc \theta = \frac{H}{O} = \frac{1}{y}$

c. $\cos \theta = \frac{A}{H} = x$

d. $\sec \theta = \frac{H}{A} = \frac{1}{x}$

e. $\tan \theta = \frac{O}{A} = \frac{y}{x}$

f. $\cot \theta = \frac{A}{O} = \frac{x}{y}$