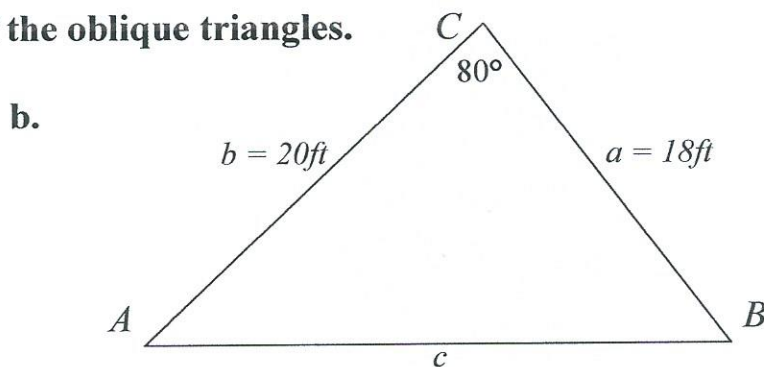
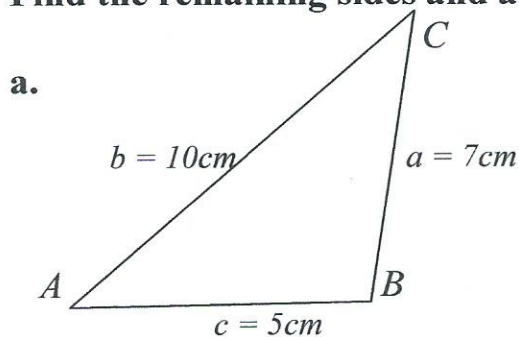


Practice 9.3: The Law of Cosines

1. Find the remaining sides and angles of the oblique triangles.



(SSS) c. $a = 55\text{mi}, b = 25\text{mi}, c = 72\text{mi}$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc} = \frac{25^2 + 72^2 - 55^2}{2 \cdot 25 \cdot 72}$$

$$\cos A = \frac{58}{75} : \cos^{-1}\left(\frac{58}{75}\right) = A = \underline{39.3^\circ}$$

$$\cos^{-1}\left(\frac{25^2 + 55^2 - 72^2}{2 \cdot 25 \cdot 55}\right) = C = \underline{123.9^\circ}$$

$$\cos^{-1}\left(\frac{55^2 + 72^2 - 25^2}{2 \cdot 55 \cdot 72}\right) = B = \underline{16.7^\circ}$$

e. $a = 4\text{in}, b = 9\text{in}, c = 10\text{in}$



d. $A = 120^\circ, b = 3\text{km}, c = 10\text{km}$

f. $C = 55^\circ, b = 3\text{m}, a = 10\text{m}$

~~$$a^2 = b^2 + c^2 - 2bc \cdot \cos C$$~~

$$c^2 = b^2 + a^2 - 2ba \cos C$$

$$= 3^2 + 10^2 - 2 \cdot 3 \cdot 10 \cdot \cos 55^\circ$$

$$c^2 = 74.59 \quad c = \underline{8.6}$$

$$\frac{\sin 55^\circ}{8.6} = \frac{\sin B}{3} = \frac{\sin a}{10}$$

$$\sin B = 3 \sin 55^\circ / 8.6 \quad \sin^{-1}\left(\frac{3 \sin 55^\circ}{8.6}\right) = B = \underline{16.7^\circ}$$

$$\sin^{-1}\left(\frac{10 \sin 55^\circ}{8.6}\right) = A = \underline{72.3^\circ}$$