

## Practice 8.4:      **Sum & Difference Formulas**

Use the Sum and Difference Formulas to find the exact values of the following trig functions. Show your work.

1.  $\cos 75^\circ$

use  $30^\circ + 45^\circ = 75^\circ$

2.  $\sin 15^\circ = \sin(45^\circ - 30^\circ) = \sin 45^\circ \cos 30^\circ - \cos 45^\circ \sin 30^\circ$  use  $45^\circ - 30^\circ = 15^\circ$

$$\frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} - \frac{\sqrt{2}}{2} \cdot \frac{1}{2}$$

$$\frac{\sqrt{6}}{4} - \frac{\sqrt{2}}{4} = \frac{\sqrt{6} - \sqrt{2}}{4}$$

3.  $\tan 105^\circ$

use  $60^\circ + 45^\circ = 105^\circ$

4.  $\cos 195^\circ$

use  $225^\circ - 30^\circ = 195^\circ$

5.  $\sin \frac{7\pi}{12}$

use  $\frac{\pi}{3} + \frac{\pi}{4} = \frac{7\pi}{12}$

$$6. \tan 255^\circ = \frac{\tan(300^\circ) - \tan 45^\circ}{1 + \tan 300^\circ \tan 45^\circ} = \frac{-\sqrt{3} - 1}{1 + (-\sqrt{3})(1)}$$

$$= \frac{-1 - \sqrt{3}}{1 - \sqrt{3}}$$

use  $300^\circ - 45^\circ = 255^\circ$

can be simplified more

7. Use the Sum and Difference Formulas to write the trig function of an angle.

a.  $\cos 25^\circ \cos 15^\circ - \sin 25^\circ \sin 15^\circ =$

b.  $\sin 140^\circ \cos 50^\circ - \cos 140^\circ \sin 50^\circ = \sin(140^\circ - 50^\circ) = \sin 90^\circ = 1$

c.  $\frac{\tan 325^\circ - \tan 86^\circ}{1 + \tan 325^\circ \tan 86^\circ} =$

$$d. \cos \frac{\pi}{7} \cos \frac{\pi}{5} - \sin \frac{\pi}{7} \sin \frac{\pi}{5} = \cos\left(\frac{\pi}{7} + \frac{\pi}{5}\right) = \cos\left(\frac{5\pi}{35} + \frac{7\pi}{35}\right) = \cos \frac{12\pi}{35}$$