

Math 112: #17 A/B/C/DA) Find *all* the solutions in $[0, 2\pi)$ to the equation $2\sin^2 x - \cos x = 1$.

$$2(1 - \cos^2 x) - \cos x = 1$$

$$2 - 2\cos^2 x - \cos x = 1$$

-2 + 2\cos^2 x + \cos x -2 + 2\cos^2 x + \cos x

$$0 = 2\cos^2 x + \cos x - 1$$

$$0 = (2\cos x - 1)(\cos x + 1)$$

$$2\cos x - 1 = 0 \quad \cos x + 1 = 0$$

$$\cos x = \frac{1}{2} \quad \cos x = -1$$

$\pi/3, 5\pi/3$ π

$$x = \boxed{\pi/3, \pi, 5\pi/3}$$

B) Find *all* the solutions in $[0, 2\pi)$ to the equation $2\cos^2 x - 7\cos x = -3$.

$$2\cos^2 x - 7\cos x + 3 = 0$$

$$(2\cos x - 1)(\cos x - 3) = 0$$

$$2\cos x - 1 = 0 \quad \cos x - 3 = 0$$

$$\cos x = \frac{1}{2} \quad \cos x = 3$$

$\pi/3, 5\pi/3$ no solution

$$\boxed{\pi/3, 5\pi/3}$$

C) Find *all* the solutions in $[0, 2\pi)$ to the equation $2\cos^2 x + \sin x = 1$.

$$2(1 - \sin^2 x) + \sin x = 1$$

$$2 - 2\sin^2 x + \sin x = 1$$

$$0 = 2\sin^2 x - \sin x - 1$$

$$0 = (\sin x - 1)(2\sin x + 1)$$

$$\sin x - 1 = 0 \quad 2\sin x + 1 = 0$$

$$\sin x = 1 \quad \sin x = -\frac{1}{2}$$

$$x = \frac{\pi}{2}$$

$$x = \frac{7\pi}{6}$$

$$x = \frac{11\pi}{6}$$

$$\frac{\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6}$$

D) Find *all* the solutions in $[0, 2\pi)$ to the equation

$$2\sin x \cos x - \sqrt{3} \cos x = 0$$

$$\cos x (2\sin x - \sqrt{3}) = 0$$

$$\cos x = 0$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$2\sin x - \sqrt{3} = 0$$

$$\sin x = \frac{\sqrt{3}}{2}$$

$$\frac{\pi}{3}, \frac{2\pi}{3}$$

$$\frac{\pi}{3}, \frac{\pi}{2}, \frac{2\pi}{3}, \frac{3\pi}{2}$$